



Calculation Policy

for

Mathematics



The following calculation policy has been devised to meet the requirements of the National Curriculum 2014 for the teaching and learning of mathematics, and is also designed to give pupils a consistent and smooth progression of learning in calculations across the Key Stage 1 and 2 phases. Please note that early learning in number and calculation in Reception follows the 'Development Matters' EYFS document, and this calculation policy is designed to build on progressively from the content and methods established in the Early Years Foundation Stage.

Age stage expectations

The calculation policy is organised according to age stage expectations as set out in the National Curriculum 2014 and the expectation is that the majority of pupils will move through the programmes of study at broadly the same pace. However, decisions about when to progress should always be based on the security of pupils' understanding and their readiness to progress to the next stage. Pupils who grasp concepts rapidly should be challenged through being offered rich and sophisticated problems before any acceleration through new content. Those who are not sufficiently fluent with earlier material should consolidate their understanding, including through additional practice, before moving on

Providing a context for calculation:

It is important that any type of calculation is given a real life context or problem solving approach to help build children's understanding of the purpose of calculation, and to help them recognise when to use certain operations and methods when faced with problems. This must be a priority within calculation lessons.



Choosing a calculation method:

Children need to be taught and encouraged to use the following processes in deciding what approach they will take to a calculation, to ensure they select the most appropriate method for the numbers involved.

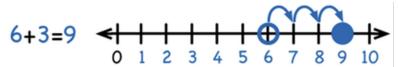
Approximate
Calculate
Check





Add one-digit and two-digit numbers to 20

Use numbered number lines to add, by counting on in ones. Encourage children to start with the larger number and count on.



Children should:

$\ \square$ Have access to a wide range of counting	equipment, e	everyday objects,	number tracks	and number
lines, and be shown numbers in different co	ontexts.			

□ Read and write the addition	(+) and ea	juals (=) sic	ns within	number	sentences.
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□ Interpret addition number sente	ences and solve missing box problems,	using concrete objects and
number line addition to solve them	$1:8+3= \Pi 15+4= \Pi 5+3+1= \Pi$	

This builds on from prior learning of adding by combining two sets of objects into one group (5 cubes and 3 cubes) in Early Years.

Bead strings or bead bars can be used to illustrate addition including bridging through ten by counting on 2 then counting on 3.

8 + 5

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line

Key skills for addition at Y1:

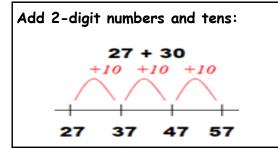
- □ Count, read and write numbers to 100 in numerals, incl. 1—20 in words
- $\ \square$ Represent and use number bonds and related subtraction facts within 20.
- ☐ Count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number.
- \square Count in multiples of twos, fives and tens.
- □ Solve simple 1-step problems involving addition, using objects, number lines and pictorial representations.

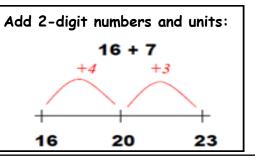




Add with two-digit numbers

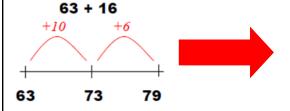
Developing mental fluency with addition and place value involving 2-digit numbers, then establish more formal methods.

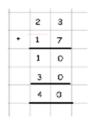




Use empty number lines, concrete equipment, hundred squares etc. to build confidence and fluency in mental addition skills.

Add pairs of 2-digit numbers, moving to the expanded column method when secure adding tens and units:





Add the units first in preparation for the compact method.

In order to carry out this method of addition:

- \Box Children need to recognise the value of the hundreds, tens and units without recording the partitioning.
- □ Pupils need to be able to add in columns.

To support understanding, pupils may physically make and carry out the calculation with Dienes Base 10 apparatus or place value counters, then compare their practical version to the written form, to help them to build an understanding of it.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

Key skills for addition at Y2:

- \square Add a 2-digit number and ones (e.g. 27 + 6)
- \square Add a 2-digit number and tens (e.g. 23 + 40)
- \square Add pairs of 2-digit numbers (e.g. 35 + 47)
- \square Add three single-digit numbers (e.g. 5 + 9 + 7)
- □ Show that adding can be done in any order (the commutative law).
- □ Recall and use addition facts to 20 fluently, and derive and use related facts up to 100.
- □ Count in steps of 2, 3 and 5 and count in tens from any number, forward and backward.
- ☐ Recognise the place value of 2-digit numbers (tens and ones)
- \Box Compare and order numbers to 100 using $\langle \rangle$ and = signs.
- $\ \square$ Read and write numbers to at least 100 in numerals and words.
- ☐ Solve problems with addition, using concrete objects, pictorial representations, involving numbers, quantities and measures, and applying mental and written methods.
- □ Identify, represent and estimate numbers using different representations including the number line.





Add numbers with up to 3-digits

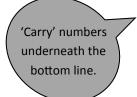
Extend the expanded column addition method to HTU + TU:

Add the units first in preparation for the compact method.

In order to carry out this method of addition:

- ☐ Children need to recognise the value of the hundreds, tens and units without recording the partitioning.
- $\hfill \square$ Pupils need to be able to add in columns.

Move to the compact column addition method, with 'carrying'.







Remind pupils that the actual value is 'three tens add seven tens', not three add seven', which equals ten tens.

Children who are very secure and confident with 3-digit expanded column addition should be moved onto the compact column addition method, being introduced to 'carrying' for the first time. Compare the expanded method to the compact column method to develop an understanding of the process and the reduced number of steps involved.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact

Key skills for addition at Y3:

- \square Read and write numbers to 1000 in numerals and words.
- ☐ Add 2-digit numbers mentally, incl. those exceeding 100.
- □ Add a three-digit number and ones mentally (175 + 8)
- □ Add a three-digit number and tens mentally (249 + 50)
- □ Add a three-digit number and hundreds mentally (381 + 400)
- \square Estimate answers to calculations, using inverse to check answers.
- \square Solve problems, including missing number problems, using number facts, place value, and more complex addition.
- ☐ Recognise place value of each digit in 3-digit numbers (hundreds, tens, ones.)
- □ Continue to practise a wide range of mental addition strategies, ie. number bonds, adding the nearest multiple of 10, 100, 100 and adjusting, using near doubles, partitioning and recombining.
- ☐ Count from 0 in multiples of 4, 8, 50. and 100.
- ☐ Compare and order numbers up to 1000.
- ☐ Find 10 or 100 more or less than a given number.





Add numbers with up to 4 digits

Move from expanded addition to the compact column method, adding units first, and 'carrying' numbers underneath the calculation. Also include money and measures contexts.

e.g. 3517 + 396 = 3913

	3	5	1	7	
+		3	9	6	
	3	9	1	3	
		1	1		A

Introduce the compact column addition method by asking children to add the two given numbers together using the method that they are familiar with (expanded column addition—see Y3). Teacher models the compact method with carrying, asking children to discuss similarities and differences and establish how it is carried out.

Add units first

'Carry' numbers underneath

Reinforce correct place value by reminding them the actual value is 5 hundreds add 3 hundreds, **Not 5 add 3**, for example.

Extend to adding 3 whole numbers e.g. 3517+ 396 + 43

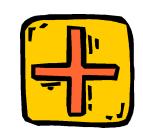
Use and apply this method to money and measurement values.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact, thousands, hundreds, digits, inverse

Key skills for addition at Y4:

- □ Select most appropriate method: mental, jottings or written and explain why.
- □ Recognise the place value of each digit in a four-digit number.
- □ Round any number to the nearest 10, 100 or 1000.
- □ Estimate and use inverse operations to check answers.
- □ Solve 2-step problems in context, deciding which operations and methods to use and why.
- ☐ Find 1000 more or less than a given number.
- □ Continue to practise a wide range of mental addition strategies, ie. number bonds, add the nearest multiple of 10, 100, 1000 and adjust, use near doubles, partitioning and recombining.
- □ Add numbers with up to 4 digits using the formal written method of column addition
- □ Solve 2-step problems in contexts, deciding which operations and methods to use and why.
- □ Estimate and use inverse operations to check answers to a calculation.





Add numbers with more than 4 digits

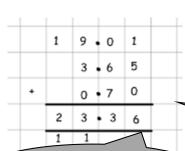
including money, measures and decimals with different numbers of decimal plac-



The decimal point should be aligned in the same way as the other place value columns, and must be in the same column in the answer.



Numbers should exceed 4 digits.



Pupils should be able to add more than two values, carefully aligning place value columns.

Say '6 tenths add 7 tenths' to reinforce place value.

Empty decimal places can be filled with zero to show the place value in each column.

Children should: Understand the place value of tenths and hundredths and use this to align numbers with different numbers of decimal places.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary,

increase, 'carry', expanded, compact, vertical, thousands, hundreds, digits, inverse & decimal places,

decimal point, tenths, hundredths, thousandths

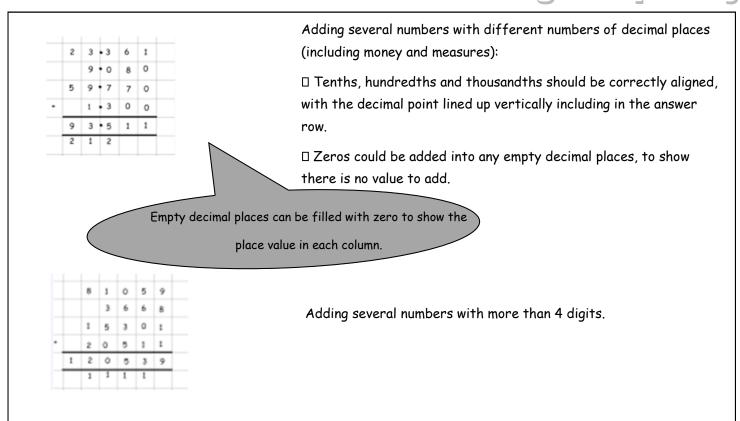
Key skills for addition at Y5:

- □ Add numbers mentally with increasingly large numbers, using and practising a range of mental strategies ie. add the nearest multiple of 10, 100, 100 and adjust; use near doubles, inverse, partitioning and re-combining; using number bonds.
- □ Use rounding to check answers and accuracy.
- □ Solve multi-step problems in contexts, deciding which operations and methods to use and why.
- □ Read, write, order and compare numbers to at least 1 million and determine the value of each digit.
- $\hfill\square$ Round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000.
- □ Add numbers with more than 4 digits using formal written method of columnar addition.





Add several numbers of increasing complexity



Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, 'carry', expanded, compact, vertical, thousands, hundreds, digits, inverse, decimal places, decimal point, tenths, hundredths, thousandths

Key skills for addition at Y6:

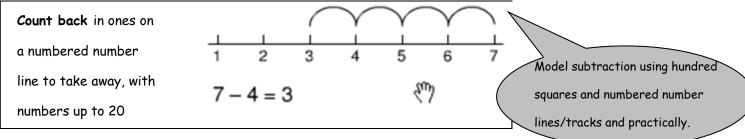
- □ Perform mental calculations, including with mixed operations and large numbers, using and practising a range of mental strategies.
- □ Solve multi-step problems in context, deciding which operations and methods to use and why.
- □ Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.
- □ Read, write, order and compare numbers up to 10 million and determine the value of each digit.
- □ Round any whole number to a required degree of accuracy.
- $\hfill\square$ Pupils understand how to add mentally with larger numbers and calculations of increasing complexity.



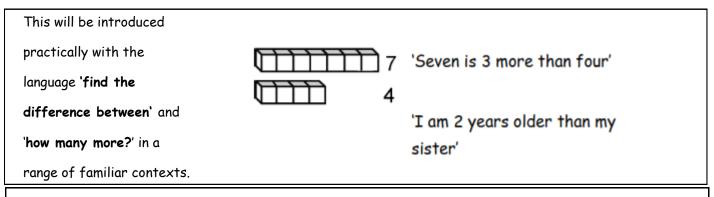
Subtract from numbers up to 20

Children consolidate understanding of subtraction practically, showing subtraction on bead strings, using cubes etc. and in familiar contexts, and are introduced to more formal recording using number lines as below:

Subtract by taking away



Find the 'difference between'



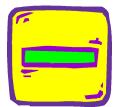
Mental subtraction

Children should start recalling subtraction facts up to **and within** 10 and 20, and should be able to subtract zero.

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_?

Key skills for subtraction at Y1:

- ☐ Given a number, say one more or one less.
- □ Count to and over 100, forward and back, from any number.
- ☐ Represent and use subtraction facts to 20 and within 20.
- □ Subtract with one-digit and two-digit numbers to 20, including zero.
- □ Solve one-step problems that involve addition and subtraction, using concrete objects (ie bead string, objects, cubes) and pictures, and missing number problems.
- ☐ Read and write numbers from 0 to 20 in numerals and words.



Subtract with 2-digit numbers

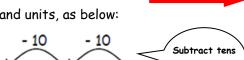
Subtract on a number line by counting back, aiming to develop mental subtraction skills.

This strategy will be used for:

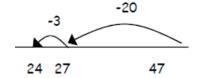
- □ 2-digit numbers subtract units (by taking away / counting back) e.g. 36—7
- □ 2-digit numbers subtract tens (by taking away / counting back) e.g. 48—30
- ☐ Subtracting pairs of 2-digit numbers (see below:)

Subtracting pairs of 2-digit numbers on a number line:

47 - 23 = 24 Partition the second number and subtract it in tens and units, as below:



Move towards more efficient jumps back, as below:



24 25 26 27 37 47

Then subtract units.

Combine methods with use of a hundred square to reinforce understanding of number value and order.

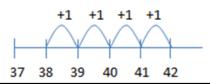
Teaching children to **bridge through ten** can help them to become more efficient, for example 42—25:





Mental strategy - subtract numbers close together by counting on:

$$42 - 38 = 4$$



Many mental strategies are taught. Children are taught to recognise that when numbers are close together, it is more efficient to count on the difference. They need to be clear about the relationship between addition and subtraction.

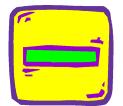
Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units

Key skills for subtraction at Y2:

- ☐ Recognise the place value of each digit in a two-digit number.
- □ Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100.
- □ Subtract using concrete objects, pictorial representations, 100 squares and mentally, including:
- a two-digit number and ones, a two-digit number and tens, and two two-digit numbers.
- ☐ Show that subtraction of one number from another cannot be done in any order.
- ☐ Recognise and use inverse relationship between addition and subtraction, using this to check calculations and missing number problems.
- □ Solve simple addition and subtraction problems including measures, using concrete objects, pictorial representation, and also applying their increasing knowledge of mental and written methods.
- ☐ Read and write numbers to at least 100 in numerals and in words.

it.

SUBTRACTION



Subtracting with 2 and 3-digit numbers

STEP 1: introduce 'exchanging' through practical subtraction.

Make the larger number with

Base 10, then subtract 47 from

67 0 + 12 - 4 0 + 7 2 0 + 5 = 2 5

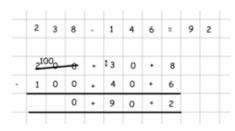
77 78 79 80 81 82

Before subtracting '7' from the 72 blocks, t will need to exchange a row of 10 for ten units. Then subtract 7, and subtract 4 tens.

72 - 47

Expanded column subtraction method

STEP 2: Once pupils are secure with the understanding of 'exchanging', they can use the partitioned column method to subtract any 2 and 3-digit numbers.



Can I do it in my head using a mental strategy?

Could I use some jottings to help me?

Should I use a written method to work it out?

Use vocabulary 'steal' or 'take' not 'borrow'.

Counting on as a mental strategy for subtraction:

Because counting on in tens is the way we use a 100 square.

Continue to reinforce counting on as a strategy for close-together numbers (e.g. 121-118), and also for numbers that are "nearly" multiples of 10, 100, 1000 or £s, which make it easier to count on (e.g. 102-89, 131-79, or calculating change from £1 etc.).

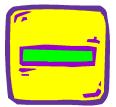
 \Box Start at the smaller number and count on in tens first, then count on in units to find the rest of the difference:

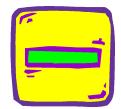
57

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit

Key skills for subtraction at Y3:

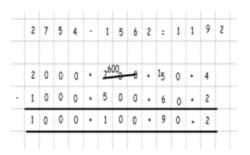
- □ Subtract mentally a: 3-digit number and ones, 3-digit number and tens, 3-digit number and hundreds .
- \square Estimate answers and use inverse operations to check.
- ☐ Solve problems, including missing number problems.
- \square Find 10 or 100 more or less than a given number.
- \square Recognise the place value of each digit in a 3-digit number .
- □ Counting up differences as a mental strategy when numbers are close together or near multiples of 10
- \square Read and write numbers up to 1000 in numerals and words.
- □ Start at the smaller number and count on in tens first, then count on in units to find the rest of the difference:
- □ Practise mental subtraction strategies, such as subtracting near multiples of 10 and adjusting (e.g. subtracting 19 or
- 21), and select most appropriate methods to subtract, explaining why.





Subtract with up to 4-digit numbers

Partitioned column subtraction with 'exchanging' (decomposition):



As introduced in Y3, but moving towards more complex numbers and values. Use **place value counters** to reinforce 'exchanging'.

Subtracting money: partition

into £1 + 30 + 5 for example.

Compact column subtraction

	2	67	15	4
-	1	5	6	2
	1	1	9	2

To introduce the compact method, ask children to perform a subtraction calculation with the familiar partitioned column subtraction then display the compact version for the calculation they have done. Ask pupils to consider how it relates to the method they know, what is similar and what is different, to develop an understanding of it.

Give plenty of opportunities to apply this to money and measures.

Always encourage children to consider the best method for the numbers involved— mental, counting on, counting back or written method.

Mental strategies

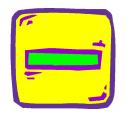
A variety of mental strategies must be taught and practised, including counting on to find the difference where numbers are closer together, or where it is easier to count on.

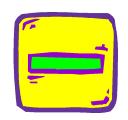
Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit,

inverse

Key skills for subtraction at y4:

- □ Subtract by counting on where numbers are close together or they are near to multiples of 10, 100 etc.
- ☐ Children select the most appropriate and efficient methods for given subtraction calculations.
- ☐ Estimate and use inverse operations to check answers.
- □ Solve addition and subtraction 2-step problems, choosing which operations and methods to use and why.
- □ Solve simple measure and money problems involving fractions and decimals to two decimal places.
- ☐ Find 1000 more or less than a given number.
- □ Count backwards through zero, including negative numbers.
- □ Recognise place value of each digit in a 4-digit number Round any number to the nearest 10, 100 or 1000
- □ Solve number and practical problems that involve the above, with increasingly large positive numbers.





Subtract with at least 4-digit numbers

including money, measures, decimals.

Compact column subtraction

(with 'exchanging').

22-	10 ₂ -	¹o	4 8€	16
	2	1	z	8
2	8	9	2	8

Children who are still not secure with number facts and place value will need to remain on the partitioned column method until ready for the compact method.

Subtracting with larger integers.



Subtract with decimal values, including mixtures of integers and decimals, aligning the decimal point.

Create lots of opportunities for subtracting and finding differences with money and measures.

Add a 'zero' in any empty decimal places to aid understanding of what to subtract in that column.

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance

between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decimal

Key skills for subtraction at Y5:

- □ Subtract numbers mentally with increasingly large numbers .
- \square Use rounding and estimation to check answers to calculations and determine, in a range of contexts, levels of accuracy .
- □ Solve addition and subtraction multi-step problems in context, deciding which operations and methods to use and why.
- ☐ Read, write, order and compare numbers to at least 1 million and determine the value of each digit.
- □ Count forwards or backwards in steps of powers of 10 for any given number up to 1 million.
- □ Interpret negative numbers in context, counting forwards and backwards with positive and negative integers through 0.
- \square Round any number up to 1 million to the nearest 10, 100, 1000, 10 000 and 100 000.



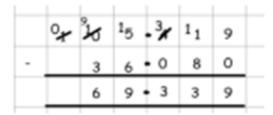


Subtracting with increasingly large and more complex numbers and decimal values

	9	14	°10°	16	9	9
-		8	9	9	4	9
		6	0	7	5	0

Using the compact column method to subtract more complex integers

Using the compact column method tosubtract money and measures, including decimals with different numbers of decimal places.



Empty decimal places can be filled with **zero** to show the place value in each column.

Pupils should be able to apply their knowledge of a range of mental strategies, mental recall skills, and informal and formal written methods when selecting the most appropriate method to work out subtraction problems.

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, distance between, how many more, how many fewer / less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decimal

Key skills for subtraction at Y6:

- □ Solve addition and subtraction multi-step problems in context, deciding which operations and methods to use and why.
- □ Read, write, order and compare numbers up to 10 million and determine the value of each digit
- □ Round any whole number to a required degree of accuracy
- $\hfill \Box$ Use negative numbers in context, and calculate intervals across zero.
- □ Children need to utilise and consider a range of mental subtraction strategies, jottings and written methods before choosing how to calculate.



MULTIPLICATION Year 1

Multiply with concrete objects, arrays and pictorial representations.

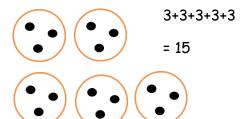
How many legs will 3 teddies have?



There are 3 sweets in one bag.

How many sweets are in $5\ \text{bags}$

altogether?



Give children experience of counting equal group of objects in 2s, 5s and 10s.

Present practical problem solving activities involving counting equal sets or groups, as above.

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count

Key skills for multiplication at Y1:

Count in multiples of 2, 5 and 10.

Solve one-step problems involving multiplication, by calculating the answer using concrete objects,

pictorial representations and arrays with the support of the teacher.

Make connections between arrays, number patterns, and counting in twos, fives and tens.

Begin to understand doubling using concrete objects and pictorial representations.



MULTIPLICATION

Year 2



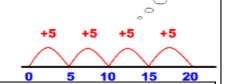
Multiply using arrays and repeated addition

(using at least 2s, 5s and 10s)

Use repeated addition on a number line:

Starting from zero, make equal jumps up on a number line to work out multiplication facts and write multiplication statements using x and z signs.





 $4 \times 5 = 20$

Use arrays:



$$5 \times 3 = 15$$

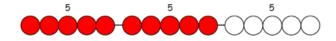
4 X 5 =

$$3 \times 5 = 15$$

$$5 \times 3 = 3 + 3 + 3 + 3 = 15$$

Use arrays to help teach children to understand the commutative law of multiplication, and give examples such as $3 \times _{--} = 6$. $5 \times 3 = 5 + 5 + 5$

Use practical apparatus:



Use mental recall:

□ Children should begin to recall multiplication facts for 2, 5 and 10 times tables through practice in counting and understanding of the operation.

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times...

Key skills for multiplication at Y2:

- \square Count in steps of 2, 3 and 5 from zero, and in 10s from any number.
- □ Recall and use multiplication facts from the 2, 5 and 10 multiplication tables, including recognising odds and evens.
- \square Write and calculate number statements using the x and = signs.
- ☐ Show that multiplication can be done in any order (commutative).
- \square Solve a range of problems involving multiplication, using concrete objects, arrays, repeated addition, mental methods, and multiplication facts.
- □ Pupils use a variety of language to discuss and describe multiplication.



Eq.

MULTIPLICATION Year 3

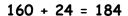


Multiply 2-digits by a single digit number

Introduce the grid method for multiplying 2-digit by single-digits:

23 x 8 = 184

X	20	3
8	160	24



Progress to expanded column multiplication

		2	3	
		2		
X			8	
		2	4	
	1	6	0	
	1	8	4	

Introduce the grid method with children physically making an array to represent the calculation (e.g. make 8 lots of 23 with 10s and 1s place value counters), then translate this to grid method format.

To do this, children must be able to:

- □ Partition numbers into tens and units
- \square Multiply multiples of ten by a single digit (e.g. 20 \times 4) using their knowledge of multiplication facts and place value
- □ Recall and work out multiplication facts in the 2, 3, 4, 5, 8 and 10 times tables.
- \Box Work out multiplication facts not known by repeated addition or other taught mental strategies (e.g. by commutative law, working out near multiples and adjusting, using doubling etc.) Strategies to support this are repeated addition using a number line, bead bars and arrays: +4 +4 +4



 $9 \times 4 = 36$



Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times, _times as big as, once, twice, three times..., partition, grid method, multiple, product, tens, units, value

Key skills for multiplication:

- □ Recall and use multiplication facts for the 2, 3, 4, 5, 8 and 10 multiplication tables, and multiply multiples of 10.
- ☐ Write and calculate number statements using the multiplication tables they know, including 2-digit x single-digit, drawing upon mental methods, and progressing to reliable written methods.
- □ Solve multiplication problems, including missing number problems.
- \Box Develop mental strategies using commutativity (e.g. $4 \times 12 \times 5 = 4 \times 5 \times 12 = 20 \times 12 = 240$)
- □ Solve simple problems in contexts, deciding which operations and methods to use.
- \Box Develop efficient mental methods to solve a range of problems e.g using commutativity (4 × 12 × 5 = 4 ×
- $5 \times 12 = 20 \times 12 = 240$) and for missing number problems $\square \times 5 = 20$, $3 \times \square = 18$, $\square \times \square = 32$



MULTIPLICATION Year 4.

Multiply 2 and 3-digits by a single digit

Using all mul-

tiplication tables up

Developing the grid method:

Eq. $136 \times 5 = 680$

X	100	30	6
5	500	150	30

	5	0	0	
	2	5	0	Encourage column addition to add
+		3	0	
	6	8	0	accurately.

Developing the expanded column method:

	3	2	7
х			4
		2	8
		8	0
1	2	0	0
1	3	0	8
	1		



Move onto **short multiplication** (see Y5) if and when children are confident and accurate multiplying 2 and 3-digit numbers by a single digit this way, **and** are already confident in "carrying" for written addition.

Children should be able to:

 \Box Approximate before they calculate, and make this a regular part of their calculating, going back to the approximation to check the reasonableness of their answer. e.g: -346×9 is approximately $350 \times 10 = 3500$

Record an approximation to check the final answer against.

- ☐ Multiply multiples of ten and one hundred by a single-digit, using their multiplication table knowledge.
- \square Recall all times tables up to 12 x 12

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, groups of, sets of, lots of, equal groups, times, multiply, times, as big as, once, twice, three times... partition, grid method, total, multiple, product, sets of, inverse

Key skills for multiplication at Y4:

- \square Count in multiples of 6, 7, 9, 25 and 1000
- \square Recall multiplication facts for all multiplication tables up to 12 x 12.
- □ Recognise place value of digits in up to 4-digit numbers.
- □ Use place value, known facts and derived facts to multiply mentally.

Use commutativity and other strategies mentally $3 \times 6 = 6 \times 3$, $2 \times 6 \times 5 = 10 \times 6$, $39 \times 7 = 30 \times 7 + 9 \times 7$.

- □ Solve problems with increasingly complex multiplication in a range of contexts.
- \square Count in multiples of 6, 7, 9, 25 and 1000
- □ Recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones)



MULTIPLICATION Year 5



Multiply up to 4-digits by 1 or 2 digits

Extend expanded column multiplication to TU x TU

-		-	
	1	4	
×	2	6	
	2	4	
	6	0	
	8	0	
2	0	0	
3	6	4	
1			

Introducing column multiplication Short multiplication for multiplying by a single digit



Introduce long multiplication for multiplying by 2 digits

_	х	10	8
	10	100	80
	3	30	24

	1	8	
x	1	3	
	5	4	
1	8	0	
2	3	4	
1			

Moving towards more complex numbers:

	1	2	3	4
×			1	6
	7	4	0	4
1	1 2	2 3	2 4	0
1	9	7	4	4
$\overline{}$				$\overline{}$

	3	6	5	2
×				8
2	9	2	1	6
	5	4	1	

Pupils could be asked to work out a given calculation using the grid, and then compare it to 'your' column method. What are the similarities and differences? Unpick the steps and show how it reduces the steps.

18 \times 3 on the 1st row (8 \times 3 = 24, carrying the 2 for twenty, then "1" \times 3). 18 \times 10 on the 2nd row. Put a zero in units first, then say 8 \times 1, and 1 \times 1.

Key vocabulary groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, _times as big as, once, twice, three times..., partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short/long multiplication, 'carry'

Key skills for multiplication at Y5:

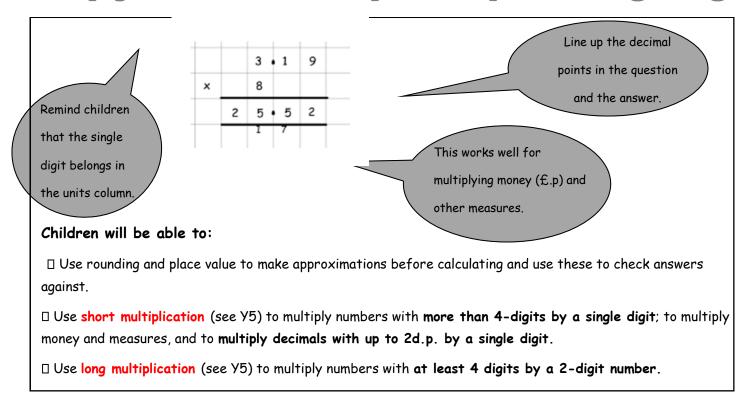
Identify multiples and factors, using knowledge of multiplication tables to 12×12 . Solve problems where larger numbers are decomposed into their factors



MULTIPLICATION Year 6



Short and long multiplication as in Y5, and multiply decimals with up to 2 d.p bu a single digit



Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times... partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short / long multiplication, "carry", tenths, hundredths, decimal

Key skills for multiplication at Y6:

- \square Recall multiplication facts for all times tables up to 12 x 12 (as Y4 and Y5).
- □ Multiply multi-digit numbers, up to 4-digit x 2-digit using long multiplication.
- ☐ Perform mental calculations with mixed operations and large numbers.
- □ Solve multi-step problems in a range of contexts, choosing appropriate combinations of operations and methods.
- ☐ Estimate answers using round and approximation and determine levels of accuracy.
- □ Round any integer to a required degree of accuracy.

DIVISION Year 1 Group and share small quantities

Using objects, diagrams and pictorial representations to solve problems involving both grouping and sharing.

How many groups of 4 can be made with 12 stars? = 3

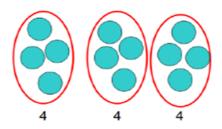
Grouping:







Sharing:



12 shared between 3 is 4

Example division problem in a familiar context:

There are 6 pupils on this table and there are 18 pieces of fruit to share between us. If we share them equally, how many will we each get?

Can they work it out and give a division statement...?

"18 shared between 6 people

gives you 3 each."

Pupils should:

□ use lots of practical apparatus, arrays and picture representations

□ Be taught to understand the difference between "grouping" objects (How many groups of 2 can you make?) and "sharing" (Share these sweets between 2 people)

 \square Be able to count in multiples of 2s, 5s and 10s.

☐ Find half of a group of objects by sharing into 2 equal groups.

Key Vocabulary: share, share equally, one each, two each..., group, groups of, lots of, array

Key number skills needed for division at Y1:

□ Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations arrays with the support of the teacher

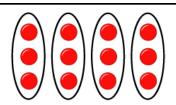
☐ Through grouping and sharing small quantities, pupils begin to understand, division, and finding simple fractions of objects, numbers and quantities.

 $\hfill\square$ They make connections between arrays, number patterns, and counting in twos, fives and tens.

• UIVISIUN • Year 2 • Group and share small quantities

Use objects, arrays, diagrams and pictorial representations, and grouping on a number line.

Arrays:



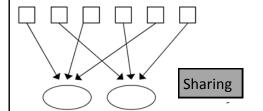
This represents $12 \div 3$, posed as how many groups of 3 are in 12? Pupils should also show that the same array can represent $12 \div 4 = 3$ if grouped horizontally.

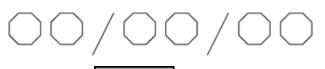
 $12 \div 3 = 4$

Know and understand sharing and grouping:

6 sweets shared between 2 people, how many do they each get?

There are 6 sweets, how many people can have 2 sweets each?



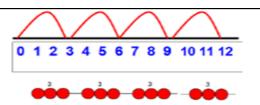


Grouping

Children should be taught to recognise whether problems require sharing or grouping.

Grouping using a number line:

Group from zero in equal jumps of the divisor to find out "how many groups of $_$ in $_$?". Pupils could and using a bead string or practical apparatus to work out problems like 'A CD costs £3. How many CDs can I buy with £12?' This is an important method todevelop understanding of division as grouping.



 $12 \pm 3 = 4$

Pose 12 ÷ 3 as 'How many groups of 3 are in 12?'

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over

Key number skills needed for division at Y2:

- \square Count in steps of 2, 3, and 5 from 0
- ☐ Recall and use multiplication and division facts for the **2**, **5 and 10** multiplication tables, including recognising odd and even numbers.
- \Box Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the x, \div and = signs.
- \Box Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- □ Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

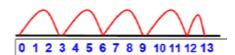


Divide 2-digit numbers by a single digit

(where there is no remainder in the final answer)

Grouping on a number line:

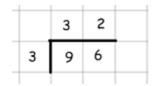
13 ÷ 3 =



STEP 1: Children continue to work out unknown division facts by grouping on a number line from zero. They are also now taught the concept of remainders, as in the example. This should be introduced practically and with arrays, as well as being translated to a number line. Children should work towards calculating some basic division facts with remainders mentally for the 2s, 3s, 4s, 5s, 8s and 10s, ready for 'carrying' remainders across within the short division method.

Short division: Limit num-

bers to **NO** remainders in the answer **OR** carried (each digit must be c



STEP 2: Once children are secure with division as grouping and demonstrate this using number lines, arrays etc., short division for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.

Remind children of correct place value, that 96 is equal to 90 and 6, but in short division, pose:

 \square How many 3's in 9? = 3, and record it above the 9 tens.

 \square How many 3's in 6? = 2, and record it above the 6 units.

Short division: Limit

numbers to **NO** remainders in the final answer, but with remainders occurring within the calculation.

STEP 3: Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation (e.g. 96†4), and be taught to 'carry' the remainder onto the next digit.

If needed, children should use the number line to work out individual division facts that occur which they are not yet able to recall mentally.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple

Key number skills needed for division at Y3:

- \square Recall and use multiplication and division facts for the 2, 3, 4, 5, 8 and 10 multiplication tables (through doubling, Connect the 2, 4 and 8s).
- ☐ Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.
- □ Solve problems, in contexts, and including missing number problems, involving multiplication and division.
- \square Pupils develop efficient mental methods, for example, using multiplication and division facts (e.g. using 3 × 2 = 6, 6 ÷ 3 = 2 and 2 = 6 ÷ 3) to derive related facts (30 × 2 = 60, so 60 ÷ 3 = 20 and 20 = 60 ÷ 3).
- □ Pupils develop reliable written methods for division, starting with calculations of 2-digit numbers by 1-digit numbers and

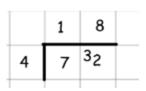
DIVISION Year 4



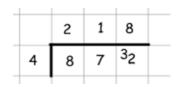
Divide up to 3-digit numbers by a single digit

(without remainders initially)

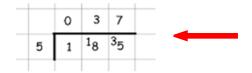
Continue to develop short division:



STEP 1: Pupils must be secure with the process of short division for dividing 2-digit numbers by a single digit (those that do not result in a final remainder—see steps in Y3), but must understand how to calculate remainders, using this to 'carry' remainders within the calculation process (see example).



STEP 2: Pupils move onto dividing numbers with upto 3-digits by a single digit, however problems and calculations provided should not result in a final answer with remainder at this stage. Children who exceed this expectation may progress to Y5 level.



When the answer for the **first column** is zero $(1 \div 5$, as in example), children could initially write a zero above to acknowledge its place, and-must always 'carry' the number (1) over to the next digit as a remainder.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, **divisible by, factor**

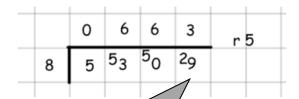
Key number skills needed for division at Y4:

- \square Recall multiplication and division facts for all numbers up to 12 \times 12.
- \square Use place value, known and derived facts to multiply and divide mentally, including: multiplying and dividing by 10 and 100 and 1.
- \square Pupils practise to become fluent in the formal written method of short division with exact answers when dividing by a one-digit number
- \square Pupils practise mental methods and extend this to three-digit numbers to derive facts, for example 200
- \times 3 = 600 so 600 ÷ 3 = 200
- □ Pupils solve two-step problems in contexts, choosing the appropriate operation, working with increasingly harder numbers. This should include correspondence questions such as three cakes shared equally between 10 children.

Year 5 Divide up to 4 digits by a single digit

including those with remainders.

Short division, including remainder answers:



Short division with remainders: Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where pupils consider the meaning of the remainder depending upon the context of the problem.

The answer to 5309 ÷ 8 could be rounded as appropriate to the problem involved.

and measure contexts.

See Y6 for how to continue the short division to give a decimal answer for children who are confident.

If children are confident and accurate:

□ Introduce **long division** for pupils who are ready to divide any number by a 2-digit number (e.g. 2678 ÷ 19). This is a Year 6 expectation—see Year 6.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor, inverse, quotient, prime number, prime factors, composite number (non-prime)

Key number skills needed for division at Y5:

- \square Recall multiplication and division facts for all numbers up to 12 x 12 (as in Y4).
- ☐ Multiply and divide numbers mentally, drawing upon known facts.
- □ Identify multiples and factors, including finding all factor pairs of a number, and common factors of two number.
- □ Solve problems involving multiplication and division where larger numbers are decomposed into their factors.
- \square Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.
- \square Use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers.
- \square Work out whether a number up to 100 is prime, and recall prime numbers to 19.
- \square Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.
- □ Use multiplication and division as inverses.
- □ Interpret non-integer answers to division by expressing results in different ways according to the context, including with remainders, as fractions, as decimals or by rounding (e.g.98÷4=24r2=24 $\frac{1}{2}$ = 24.5 $^{\sim}$ 25).
- □ Solve problems involving combinations of all four operations, including understanding of the equals sign, and including division for scaling by different fractions and problems involving simple rates.



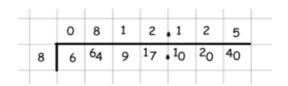




Divide at least 4 digits by both single-digit and 2-digit numbers

(including decimal numbers and quantities)

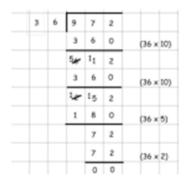
Short division, for dividing by a single digit: e.g. 6497 ÷ 8



Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as fractions, decimals, whole number remainders, or rounded numbers. Real life problem solving contexts need to be the starting point, where pupils have to consider the most appropriate way to express the remainder.

Calculating a decimal remainder: In this example, rather than expressing the remainder as \mathbf{r} 1, a decimal point is added after the units because there is still a remainder, and the one remainder is carried onto zeros after the decimal point (to show there was no decimal value in the original number). Keep dividing to an appropriate degree of accuracy for the problem being solved.

Introduce long division by chunking for dividing by 2 digits.



= <u>27</u>

Find out 'How many 36s are in 972?' by subtracting 'chunks' of 36, until zero is reached (or until there is a remainder). Teach pupils to write a 'useful list' first at the side that will help them decide what

chunks to use, e.g.:

Useful' list: 1x = 36

10x = 360

100x = 3600

Introduce the method in a simple way by limiting the choice of chunks to 'Can we use 10 lots? Can use 100 lots? As children become confident with the process, encourage more efficient chunks to get to the answer more quickly (e.g. 20x, 5x), and expand on their 'useful' lists.

Key Vocabulary: As previously, & common factor

Key number skills needed for division at Y6:

- \square Recall and use multiplication and division facts for all numbers to 12 x 12 for more complex calculations
- □ Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context. Use short division where appropriate.
- ☐ Perform mental calculations, including with mixed operations and large numbers.
- □ Identify common factors, common multiples and prime numbers.
- □ Solve problems involving all 4 operations.
- □ Use estimation to check answers to calculations and determine accuracy, in the context of a problem.
- \square Use written division methods in cases where the answer has up to two decimal places.
- □ Solve problems which require answers to be rounded to specified degrees of accuracy.